

# Announcements

1) Last Day to Drop tomorrow

11/10

# Laplace Transforms

(Chapter 7)

Back to the Brine!

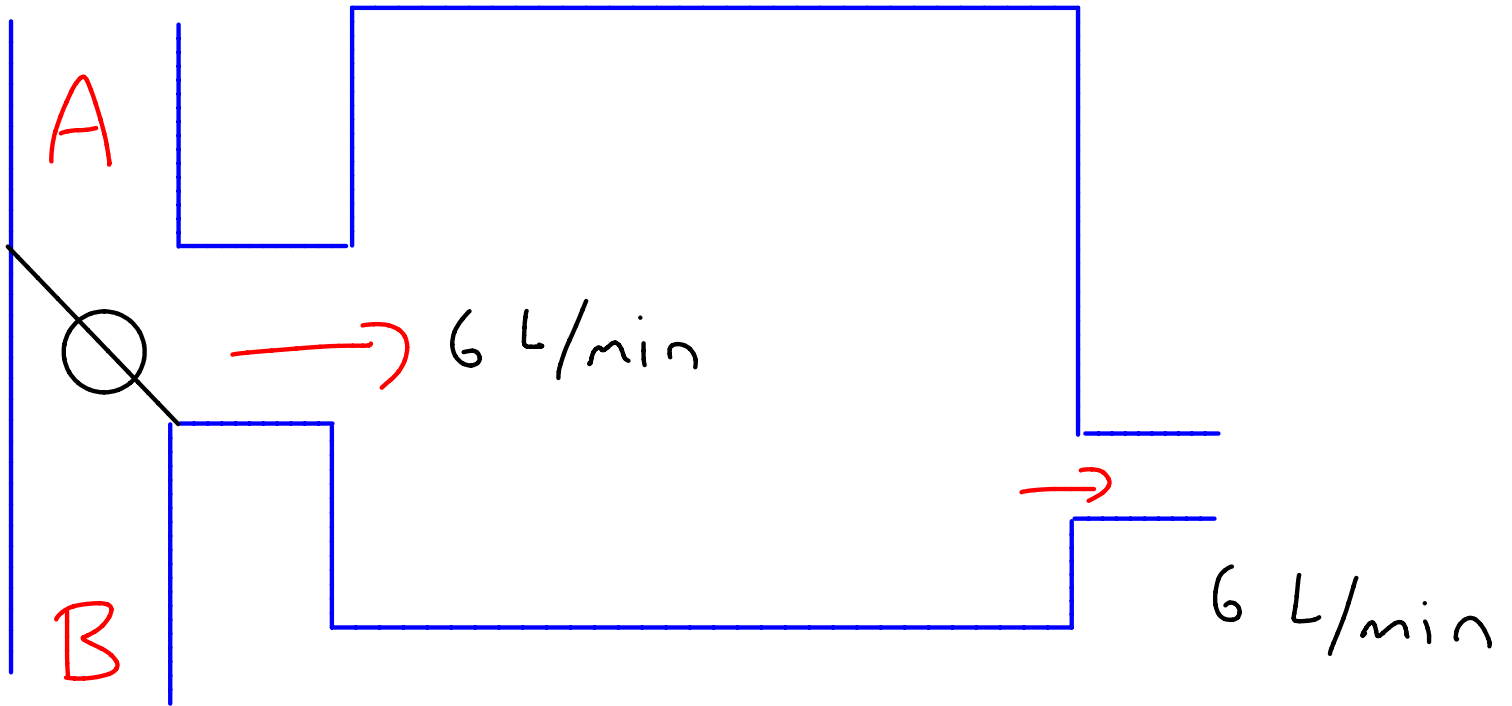
Given a tank containing  
1000 L of water in which  
30 kg of salt are dissolved.

The tank has two input  
valves, A and B,  
which can't both be open  
at the same time

Valves A and B deliver liquid at  $6 \text{ L/min}$ , but the solution from valve A contains  $.2 \text{ kg}$  of salt per liter, and the solution in valve B contains  $.4 \text{ kg}$  of salt per liter.

Liquid exits the tank at  $6 \text{ L/min}$ .

# Picture



At  $t=0$ , valve A is open. At  $t=10$ , valve A is closed and valve B is opened.

Find a formula for  $X(t)$ , the amount of salt in the tank at time  $t$ .

$$\frac{dx}{dt} = (\text{rate in}) - (\text{rate out})$$

$$= (\text{rate in}) - \frac{x(t)}{1000} \cdot 6$$

$$= (\text{rate in}) - \frac{3x(t)}{500}$$

$$= 6(?) - \frac{3x(t)}{500}$$



what goes here?

$$? = h(t) = \begin{cases} .2 \text{ kg}, & 0 \leq t < 10 \\ .4 \text{ kg}, & t \geq 10 \end{cases}$$

Since we switch from valve

A to valve B after  $t = 10$ .

$$\frac{dx}{dt} = 6h(t) - \frac{3x(t)}{500}$$

You've seen problems on the homework where you have to break functions up over the time domain - we want a better method!

**Idea:** convert differential equations to polynomial equations, solve the polynomial equation, somehow go back to the differential equation's solution.